

1	C				D
2					
3		B			
4		B			
5			C		
6					D
7			C		
Total =					

PART 1: Multiple Choice Questions (7 marks)

1. Which graphics operation is applied to give a real look to the objects

- a) Projection on 2D
- b) Viewing and clipping
- c) Rendering
- d) Hidden surface elimination

2. State the type of continuity "if directions and magnitudes of tangents are equal at the joint in parametric cubic curves"

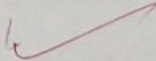
- a) G0
- b) G1
- c) C0
- d) C1

3. Identify which of the below conditions is not satisfactory for metaballs

- a) A point surrounded by a density field ✓
- b) The density increases with distance from the point ✓
- c) The density of multiple particles is summed ✓
- d) A thresholding value is also chosen, to define a solid volume. ✓

3. Identify the graphics operation that is applied to remove the distortion artifacts produced when representing a high-resolution signal at a lower resolution

- A. Aliasing
- B. Antialiasing
- C. Scan conversion
- D. Z buffering



6. In 2D-translation, a point (x, y) can move to the new position (x', y') by using the equation

- a) $x' = x + Tx$ and $y' = y + Tx$
- b) $x' = x + Tx$ and $y' = y + Ty$
- c) $X' = x + Ty$ and $Y' = y + Tx$
- d) $X' = x - Tx$ and $y' = y - Ty$



[A, B, R, L]

4. If the line is entirely within the window, then both points will have out-codes.

- a) 0100
- b) 0000
- c) 1111
- d) 1010

5. Recognize the transformation in which an object is moved from one position to another in circular path around a specified pivot point is called

- a) Translation
- b) Scaling
- c) Rotation
- d) Reflection

6. Identify the transformation in which the x and y coordinates are interchanged and their values are negated

- a) Translation
- b) Scaling
- c) Rotation
- d) Reflection

7. Identify which curves are defined by two endpoints and two other points that specify the gradient at the endpoints.?

- a) B-splines
- b) β -splines
- c) Bezier
- d) Hermit

PART-II: 8 Marks

1. Given the 2D object below. Rotate the object by 90 degrees about
 a) the origin b) on the Reference Point (10,10).

- A (10, 10)
- B (10, 25)
- C (45, 25)
- D (45, 10)

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + \begin{bmatrix} \cos 90 & -\sin 90 & 0 \\ \sin 90 & \cos 90 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} A & B & C & D \\ 10 & 10 & 45 & 45 \\ 10 & 25 & 25 & 10 \\ 1 & 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} -10 & -25 & -25 & -10 \end{bmatrix}$$

* because at point (a) the rotation is about the origin there is no need to move the shape

$$\begin{aligned}
 x' &= x \cos \theta - y \sin \theta \\
 y' &= y \cos \theta + x \sin \theta
 \end{aligned}$$

3. Identify which of the below conditions is not satisfactory for metaballs
- a) A point surrounded by a density field
 - b) The density increases with distance from the point
 - c) The density of multiple particles is summed
 - d) A thresholding value is also chosen, to define a solid volume.

4. If the line is entirely within the window, then both points will have out-codes.

- a) 0100
- b) 0000
- c) 1111
- d) 1010

5. Using Hermite curve, Polynomial can be specified by the position of, and gradient at, each endpoint of curve. The values of $X'_1 =$ _____

- A. a_0
- B. a_1
- C. $a_3 + a_2 + a_1 + a_0$
- D. $3a_3 + 2a_2 + a_1$

6. In 2D-translation, a point (x, y) can move to the new position (x', y') by using the equation

- a) $x' = x + Tx$ and $y' = y + Tx$
- b) $x' = x + Tx$ and $y' = y + Ty$
- c) $X' = x + Ty$ and $Y' = y + Tx$
- d) $X' = x - Tx$ and $y' = y - Ty$

7. Identify which curves are defined by two endpoints and two other points that specify the gradient at the endpoints?

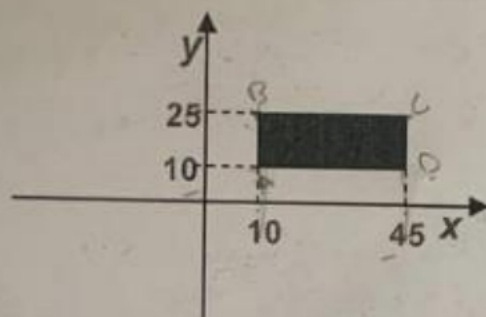
- a) B-splines
- b) β -splines
- c) Bezier
- d) Hermit

PART-II: 8 Marks

1. Given the 2D object below. Rotate the object by 120 degrees about
- a) the origin
 - b) on the Reference Point (20,20).

tran - rotate
tran +

(3 marks)



A (10, 10)

B (10, 25)

C (45, 25)

D (45, 10)

Calculate the new values and display the final result

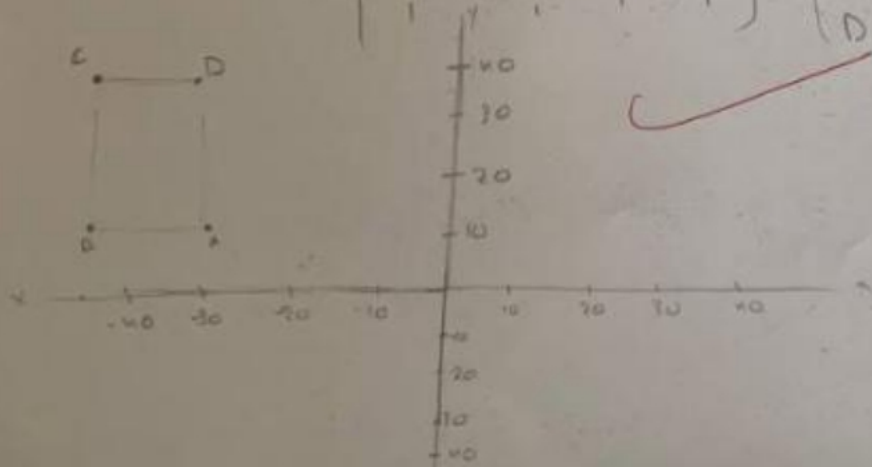
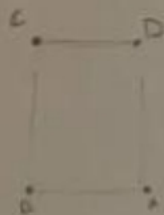
$$T_{\text{com}} = \begin{bmatrix} 1 & 0 & -10 \\ 0 & 1 & -10 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos 90 & -\sin 90 & 0 \\ \sin 90 & \cos 90 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 10 & 10 \\ 10 & 25 \\ 45 & 25 \\ 45 & 10 \end{bmatrix}$$

$$T_{\text{comp}} = \begin{bmatrix} 0 & -1 & -20 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$V' = T_{\text{comp}} \cdot V$$

$$V' = \begin{bmatrix} 0 & -1 & -20 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 10 & 10 & 45 & 45 \\ 10 & 25 & 25 & 10 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} -30 & -45 & -45 & -30 \\ 10 & 10 & 45 & 45 \\ 1 & 1 & 1 & 1 \end{bmatrix} = \begin{cases} A(-30, 10) \\ B(-45, 10) \\ C(-45, 45) \\ D(-30, 45) \end{cases}$$



Q1 120° $A(10,10)$ $B=(10,25)$ $C=(45,10)$ $D=(45,25)$

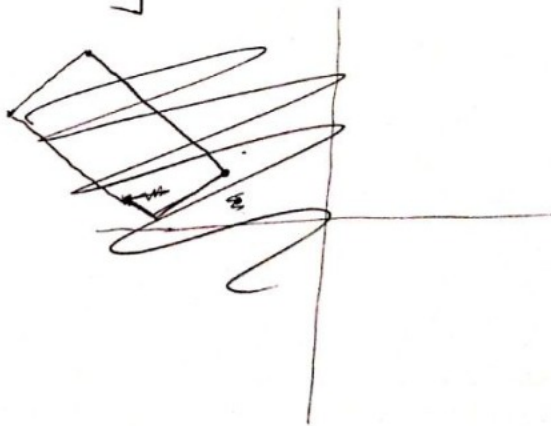
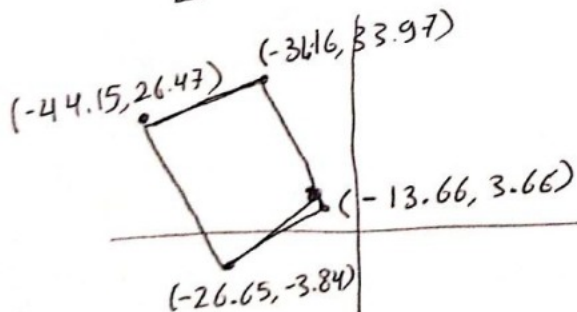
a) origin

$$V = [A \ B \ C \ D] = \begin{bmatrix} 10 & 10 & 45 & 45 \\ 10 & 25 & 10 & 25 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$T_{\text{Rotate}} = \begin{bmatrix} \cos 120 & -\sin 120 & 0 \\ \sin 120 & \cos 120 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} -0.5 & -\sqrt{3}/2 & 0 \\ \sqrt{3}/2 & -0.5 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$V' = \begin{bmatrix} -0.5 & -\sqrt{3}/2 & 0 \\ \sqrt{3}/2 & -0.5 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 10 & 10 & 45 & 45 \\ 10 & 25 & 10 & 25 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$V' = \begin{bmatrix} -13.66 & -26.65 & -31.16 & -44.15 \\ 3.66 & -3.84 & 33.97 & 26.47 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$



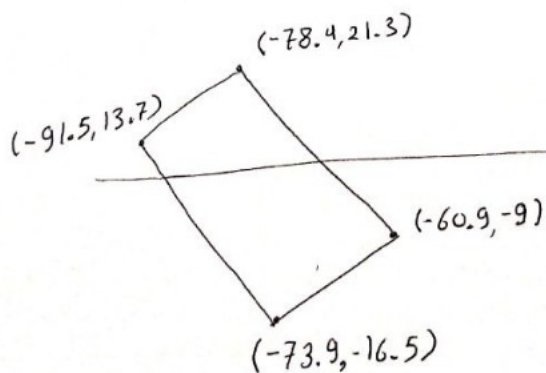
b) (20,20)

$$T_c = \begin{bmatrix} 1 & 0 & -20 \\ 0 & 1 & -20 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} -0.5 & -\sqrt{3}/2 & 0 \\ \sqrt{3}/2 & -0.5 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 20 \\ 0 & 1 & 20 \\ 0 & 0 & 1 \end{bmatrix}$$

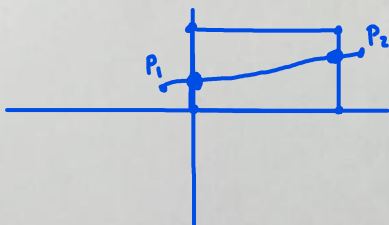
$$T_c = \begin{bmatrix} -0.5 & -0.866 & -47.32 \\ 0.866 & -0.5 & -12.68 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\vec{v} = T_c \cdot \vec{v} = \begin{bmatrix} -0.5 & -0.866 & -47.32 \\ 0.866 & -0.5 & -12.68 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 10 & 10 & 45 & 45 \\ 10 & 25 & 10 & 25 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$\vec{v} = \begin{bmatrix} -60.98 & -73.97 & -78.48 & -91.47 \\ -9.02 & -16.52 & 21.29 & 13.79 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$



- 2 Consider the line from $P_1(-1,1)$ to $P_2(12,4)$. Determine its visibility against the clipping window defined by vertices $(0,0)$, $(10,0)$, $(10,6)$, $(0,6)$ using Cohen-Sutherland algorithm (3 Marks)



$$\begin{array}{r}
 P_1 \rightarrow 0001 \quad \text{non-ZO} \\
 P_2 \rightarrow 0010 \\
 \hline
 0000 \quad \text{ZO}
 \end{array}$$

$$\begin{array}{r}
 P_1' \rightarrow 0000 \\
 P_2 \rightarrow 0010 \quad \text{non-ZO} \\
 \hline
 0000
 \end{array}$$

$$\begin{array}{r}
 P_1' \rightarrow 0000 \\
 P_2' \rightarrow 0000 \\
 \hline
 0000
 \end{array}$$

Q2.

$$P_1(-1, 1)$$

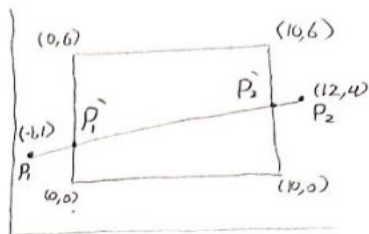
$$P_2(12, 4)$$

$$(0, 0) \quad (10, 0) \quad (10, 6) \quad (0, 6)$$

$$P_1 \rightarrow 0001$$

$$P_2 \rightarrow 0010$$

$$\text{AND} = 0000$$



Intersection point $P_1'(x_1', y_1')$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{4 - 1}{12 - (-1)} = \frac{3}{13}$$

$$\frac{3}{13} = \frac{y_1' - y_1}{x_1' - x_1} \Rightarrow \frac{3}{13} = \frac{y_1' - 1}{0 - (-1)} = y_1' - 1$$

$$y_1' = \frac{3}{13} + 1 = \frac{16}{13} = \underline{1.23}$$

$$\therefore P_1'(0, 1.23)$$

Intersection point $P_2'(x_2', y_2')$

$$m = \frac{y_2 - y_2'}{x_2 - x_2'} \rightarrow \frac{3}{13} = \frac{4 - y_2'}{12 - 10}$$

$$\frac{3}{13} = \frac{4 - y_2'}{2} \rightarrow \frac{6}{13} = 4 - y_2' \rightarrow y_2' = 4 - \frac{6}{13}$$

$$y_2' = \frac{46}{13} = 3.54$$

$$\therefore P_2'(10, 3.54)$$

$$t=0.5$$

2. Find the midpoint of a Hermite cubic spline with two end points as $X_0(3,3)$ & $X_1(8,7)$ and corresponding tangent vectors as $X_0'(0,6)$ & $X_1'(6,0)$

3. The coordinates of four control points relative to a curve are given by $P_1(1,2)$ $P_2(3,4)$ $P_3(6, 6)$ and $P_4(10,8)$. Write the equations of Beizer curve and compute Bezeir curve for step size of 0.25.

+ ↗

(2 Marks)

$$Q3. P_1(1, 2)$$

$$P_2(3, 4)$$

$$P_3(6, 6) \quad P_4(10, 8)$$

$$X_1 = 1 \quad Y_1 = 2$$

$$X_2 = 3 \quad Y_2 = 4$$

$$X_3 = 6 \quad Y_3 = 6$$

$$X_4 = 10 \quad Y_4 = 8$$

$$X: \quad X = X_4 t^3 + 3X_3 t^2(1-t) + 3X_2 t(1-t)^2 + X_1(1-t)^3$$

$$X = 10t^3 + 18t^2(1-t) + 9t(1-t)^2 + (1-t)^3$$

$$Y: \quad Y = Y_4 t^3 + 3Y_3 t^2(1-t) + 3Y_2 t(1-t)^2 + Y_1(1-t)^3$$

$$Y = 8t^3 + 18t^2(1-t) + 12t(1-t)^2 + 2(1-t)^3$$

for $t = 0.25$

$$X = 2.6875$$

$$Y = 3.5$$